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A comment on generalized $\alpha\beta$ -closed sets

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ABSTRACT

set are equivalent.

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1. Introduction

The new class *b*-closed set was introduced by Andrijevic [1]. The application of *b*-open sets had been introduced by Caldas and [afari [2]. Many results had been obtained by using the concept of b-closed sets. Also, Vinayagamoorthi and Nagaveni [3] discussed and established the concept of generalized αb -closed sets as a generalization of *b*-closed sets. We will show that the concept of *b*-closed set and a generalized αb -closed set are same. This means that all results in [3-7] are considered as the same well-known results.

Definition 1.1 [1]. Let (X, τ) be a topological spaces. A subset $A \subseteq$ *X* is said to be *b*-closed set if $int(cl(A)) \sqcap cl(int(A)) \sqsubseteq A$.

Definition 1.2 [3]. Let (X, τ) be a topological spaces. A subset $A \sqsubseteq$ X is said to be a generalized αb -closed set (briefly $g\alpha b$ -closed set) if $bcl(A) \sqsubseteq U$ whenever $A \sqsubseteq U$ and U is an α -open set.

2. Main result

Theorem 2.1. The concepts of a $g\alpha b$ -closed set and b-closed set are equivalent.

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Proof. Clearly *b*-closeness \Rightarrow g α *b*-closeness. \Box

In this note, we will show that the notions of generalized alpha b-closed ($g\alpha b$ -closed) sets and b-closed

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Conversely: let (X, τ) be a topological spaces and $A \sqsubseteq X$ be a $g\alpha b$ -closed set. We will prove that A is b-closed set, for let $x \in$ *bcl*(*A*). Since every singleton is either preopen or nowhere dense, then we have the following two cases.

Case (1): If x is preopen, then it is also b-open, $\{x\} \sqcap A \neq \emptyset$, and hence $x \in A$. Therefore $bcl(A) \sqsubseteq A$, and hence A is b-closed.

Case (2): If {*x*} is nowhere dense, then $int(cl{x}) = \emptyset$, implies $X = cl(int(X \setminus \{x\})).$ Then $X \setminus \{x\} \subseteq X = intX =$ this $int(cl(int(X \setminus \{x\})))$. Therefore $X \setminus \{x\}$ is α -open. Suppose that $x \notin A$, then $A \sqsubseteq X \setminus \{x\}$ and, since A is $g\alpha b$ -closed, we have $bcl(A) \sqsubseteq A$ *X*\{*x*\. Hence $x \notin bcl(A)$, which is a contradiction and hence $x \in A$. Therefore $bcl(A) \sqsubseteq A$, and hence A is b-closed.

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